## Exercises for seminar week IX, November 16-19, ECON3215/4215, fall 2010

## A

Consider a pure exchange economy with two consumers, $A$ and $B$, and two goods. The utility functions are:

$$
\begin{gathered}
u_{A}\left(x_{1}, x_{2}\right)=x_{1}^{a} x_{2}^{b}, \\
u_{B}\left(x_{1}, x_{2}\right)=\min \left(x_{1}, x_{2}\right) .
\end{gathered}
$$

The parameters $a$ and $b$ are both positive.
a) Calculate the Marshallian (uncompensated) demand function for each of the consumers.
b) There are 10 units of each good in the economy. Characterize the Pareto efficient (Pareto optimal) allocations. Draw an Edgeworth box to illustrate the result.
c) If $A$ initially owns the 10 units of good 1 while $B$ owns the 10 units of good 2, and the goods are traded competitively, what are the market clearing prices and the equilibrium allocation?
d) Answer part c) if initial ownership is opposite, that is, A owns the 10 units of good 2 while $B$ owns the 10 units of good 1 .
e) Assume now in additional that $a+b=\frac{1}{2}$. Find the welfare maximizing allocation when the welfare function is given by

$$
W\left(u_{A}, u_{B}\right)=u_{A}+\frac{1}{4} u_{B} .
$$

## B

Cowell problem 10.2 (page 322)

## C

Cowell problem 10.6 (page 323-324)

